

Mid-West University
Examinations Management Office
Birendranagar, Surkhet
End Semester - Examination, 2081

Subject: DE 472- Mathematical Methods in Economics II

FM: 60

Level/program: Bachelor (B.A)

Semester: VII

Time: 3 Hours

PM: 30

Candidates are required to answer the questions in their own words as far as practicable.

Attempt ALL of the following Very Short Answer Questions.

10x1=10

1. Find the first order Differential Equation of $y = 3x^2$.
2. If $P = (1, 2, -3)$ and $Q = (2, -2, 1)$ Compute $P \cdot Q$?
3. If $X = (2, 3, -2)$, Find $\|X\|$
4. Find the value of $\cos \theta$? If $P = (1, 0, 0)$ and $Q = (0, 1, 0)$.
5. How can you define equality of two points in vector spaces?
6. Let $T: \mathbb{R}^2 \rightarrow \mathbb{R}^2$ be linear Transformation defined by $T(x, y) = (x, -2y)$. Find $T(2, 4)$.
7. Find the determinant of the matrix $A = \begin{vmatrix} -8 & 8 \\ 5 & -5 \end{vmatrix}$.
8. What is the critical point?
9. What is convex function?
10. What is Optimum condition?

Attempt any THREE of the Following Short Questions.

3x8=24

11. Define order and degree of differential equation.

Find the general solution of the equations:

i. $\frac{dy}{dx} = \frac{x^2}{1+y^2}$

ii. $x^2 \frac{dy}{dx} = 2.$

12. Define Eigen value. Find the Eigen value of the given matrix: $\begin{pmatrix} 1 & 2 \\ 2 & 1 \end{pmatrix}$.

13. Define the scalar and vector projection Q onto P. Find the scalar and vector projection Q onto P, if $Q = (1, 3, 2)$ and $P = (1, 0, 1)$.

14. Determine where the graph of the function given below is concave upwards where it is concave downwards.

$$f(x) = 2x^3 - 92 + 12x - 4.$$

Attempt any TWO of the Following Long Questions.

2x13=26

15. How can you define the integral curve? Find the consumer surplus and producer surplus if the demand and the supply functions under pure competition are $D(x) = 16 - x^2$ and $S(x) = 4 + x$ respectively.
16. i. Find a vector which is orthogonal to $P = (1, 2, 3)$ with respect to vector $Q = (0, -1, 2)$ and normalized it.
ii. Let $T: \mathbb{R}^2 \rightarrow \mathbb{R}$ be a linear transformation for which $T(1, 1) = 3$, $T(0, 1) = -2$ then, find the value of $T(1, \frac{1}{2})$.
17. Examine the function for maximum or minimum
 $u(x, y) = x^3 + y^3 - 3x - 27y + 24.$
