

Mid-West University
Examinations Management Office

Final Examinations-2080

Bachelor level/ B. Sc. /2nd Semester

Time: 3 hours

Full Marks: 60

Pass Marks:30

Subject: Calculus II (MTH423/323)

Candidates are required to give their answer in their own words as far as practicable. The figures in the margin indicate full marks.

Long answer questions:

[4x6=24]

1. Find the area of the region that lies inside the circle $r = 3 \sin \theta$ and outside the cardioid $r = 1 + \sin \theta$.

2. Show that the harmonic series.

$$\sum_{n=1}^{\infty} \frac{1}{n} = 1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \dots \text{ is divergent.}$$

Or

Find the Maclaurin Series.

$$F(x) = \sum_{n=0}^{\infty} \frac{f^{(n)}(0)}{n!} x^n = f(0) + \frac{f'(0)}{1!} x + \frac{f''(0)}{2!} x^2 + \dots$$

3. If θ is the angle between the vectors $\vec{a}$ and $\vec{b}$, then find $\vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}| \cos \theta$.
4. Solve the equation $y'' + y' - 2y = x^2$.

Short answer questions:

[6x4=24]

5. Show that the surface area of a sphere of radius r is $4\pi r^2$.
6. Sketch the conic, $r = \frac{12}{2+4 \sin \theta}$.
7. Test the series $\sum_{n=1}^{\infty} (-1)^n \frac{n^3}{3^n}$ for absolute convergence.
8. Find the domain of the Bessel function of order zero defined by $J_0(x) = \sum_{n=0}^{\infty} \frac{(-1)^n x^{2n}}{2^{2n} (n!)^2}$.
9. Find parametric and symmetric equations of the line that passes through the points A (2, 4, -3) and B (3, -1, 1).
10. Find an equation of the plane through the point (2,4,1) with normal vector $\vec{n} = \langle 2, 3, 4 \rangle$. Find the intercepts and sketch the plane.

Or

Sketch the graph of the surface $z = x^2$.

Very short answer questions.

[(3x2)=12]

11. a. Define Parametric Equations and Polar equations.
b. Plot the points whose Polar coordinates are
i. $(2, -\frac{2\pi}{3})$ ii. $(-3, \frac{3\pi}{4})$
12. a. If the series $\sum_{n=1}^{\infty} a_n$ is convergent, then $\lim_{n \rightarrow \infty} a_n = 0$.
b. Define monotonic Sequences.
13. a. If direction angles of a non-zero vector $\vec{a}$ are the angles α, β and γ , that $\vec{a}$ makes with the positive x, y and z axes then prove that $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$.
b. Solve the equation $y'' + y' - 6 = 0$.

The End