

Mid-West University
Examinations Management Office

Birendranagar, Surkhet

End Semester (Alternative/Physical) Examinations -2078

Bachelor level/ B.Sc. CSIT / 2nd Semester

Time: 3 hrs

Subject : Basic Mathematics II (MATH 425)

Full Marks : 60

Pass Marks : 30

Candidates are required to give their answer in their own words as far as practicable. The figures in the margin indicate full marks.

Attempt all the Questions

[6x10 = 60]

1. a) Give an example of REF and RREF. Prove that the following system is consistent: $x_2 - 4x_3 = 8$ and $2x_1 - 3x_2 + 2x_3 = 1$ and $5x_1 - 8x_2 + 7x_3 = 1$.

b) Define power matrix . Let $A = \begin{bmatrix} 1 & 2 \\ 3 & 0 \end{bmatrix}$, find A^3 . Find the inverse matrix of $\begin{bmatrix} 3 & 1 & \cdot & 1 & 2 \\ 5 & 2 & \cdot & 2 & 3 \\ 0 & 0 & \cdot & 5 & 1 \\ 0 & 0 & \cdot & 8 & 2 \end{bmatrix}$

2. Prove that every vector has unique additive inverse.) Find the general solution of the system whose augmented matrix is :

$$\begin{bmatrix} 3 & -4 & 2 & 0 \\ -9 & 12 & -6 & 0 \\ -6 & 8 & -4 & 0 \end{bmatrix}.$$

3. Define Null space . If $X = \begin{bmatrix} -2 \\ 1 \end{bmatrix}$ and $A = \begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix}$, Is $X \in \text{Nul}A$. Find the LU factorization of $A =$

$$\begin{bmatrix} 3 & -7 & -2 & 2 \\ -3 & 5 & 1 & 0 \\ 6 & -4 & 0 & -5 \\ -9 & 5 & -5 & 12 \end{bmatrix} \text{ Use this LU factorization of } A \text{ to solve } AX = b \text{ where } b = \begin{bmatrix} -9 \\ 5 \\ 7 \\ 11 \end{bmatrix}.$$

OR

Find the angle between two vectors $u = (3, 4)$ and $v = (-8, 6)$. Find the basis for $\text{Col}A$ and $\text{Nul}A$, $A =$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

4. Define linear transformation . Let $T: P_2 \rightarrow R^2$ by $T(p) = \begin{bmatrix} p(0) \\ p(1) \end{bmatrix}$. Show that T is linear. The set $B = \{1 + t^2, t + t^2, 1 + 2t + t^2\}$ is basis for P_2 . Find the coordinate vector of $p(t) = 1 + 4t + 7t^2$ relative to B.

5. Find the characteristics equation of $A = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 2 & 5 \\ 0 & 0 & -1 \end{bmatrix}$. Let $\lambda = 7$. show that 7 is an eigenvalue of A also find the corresponding eigenvector.

OR

Define orthogonal vector . Two vectors \mathbf{u} and \mathbf{v} are orthogonal then prove $\|\mathbf{u} + \mathbf{v}\|^2 = \|\mathbf{u}\|^2 + \|\mathbf{v}\|^2$. Use the Gram-Schmidt process to produce an orthogonal basis for W where $\left\{ \begin{bmatrix} 0 \\ 4 \\ 2 \end{bmatrix}, \begin{bmatrix} 5 \\ 6 \\ -7 \end{bmatrix} \right\}$ is a basis of subspace W of \mathbf{R}^3 .

6. For what value of h in y in the plane spanned by v_1 and v_2 ? Where $v_1 = \begin{bmatrix} 1 \\ 0 \\ -2 \end{bmatrix}, v_2 = \begin{bmatrix} -3 \\ 1 \\ 8 \end{bmatrix}$ and $y = \begin{bmatrix} h \\ -5 \\ -3 \end{bmatrix}$. Show that $S = \{(x_1, x_2, x_3) \in R^3 : x_1 + 2x_2 = 0\}$ is a subspace of R^3 .

THE END